

High-Frequency Low-Distortion One-Tone and Two-Tone Signal Generation Using Arbitrary Waveform Generator

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JAPAN



Gunma University

Research Objective

Objective

Low-Distortion sine wave generation
for ADC test

Our Approach

DSP algorithm using
Arbitrary Waveform Generator

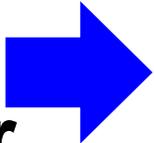
OUTLINE

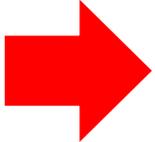
- Research background
- Phase switching algorithm
- Proposed solutions and simulations
 - High-frequency signal
 - 3rd and 5th harmonics cancellation
 - Two-tone signals
- Conclusion

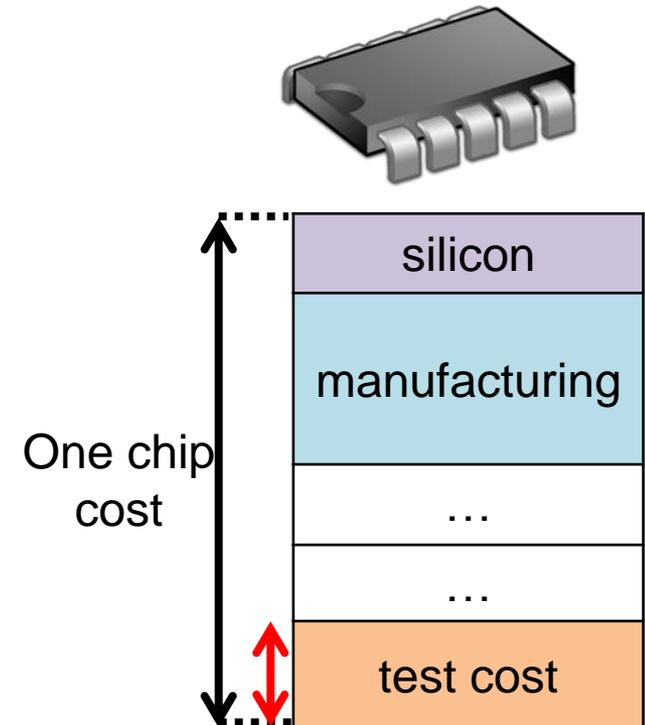
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Research Background

Silicon cost per transistor  **decreasing**

Test cost  **increasing**



Low cost test



Low cost LSI production

ADC Test Cost Using AWG



AWG : Arbitrary Waveform Generator

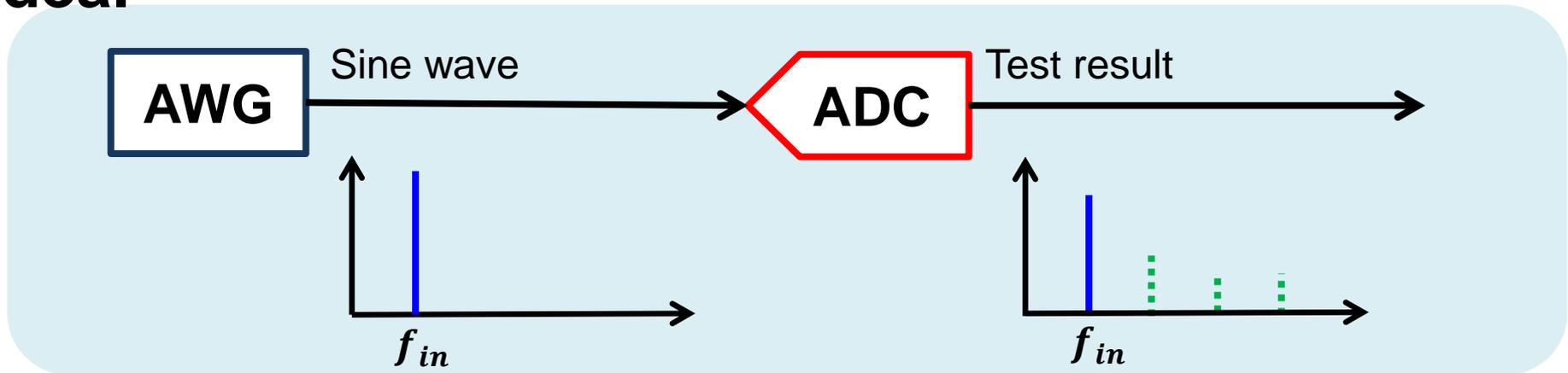
Expensive



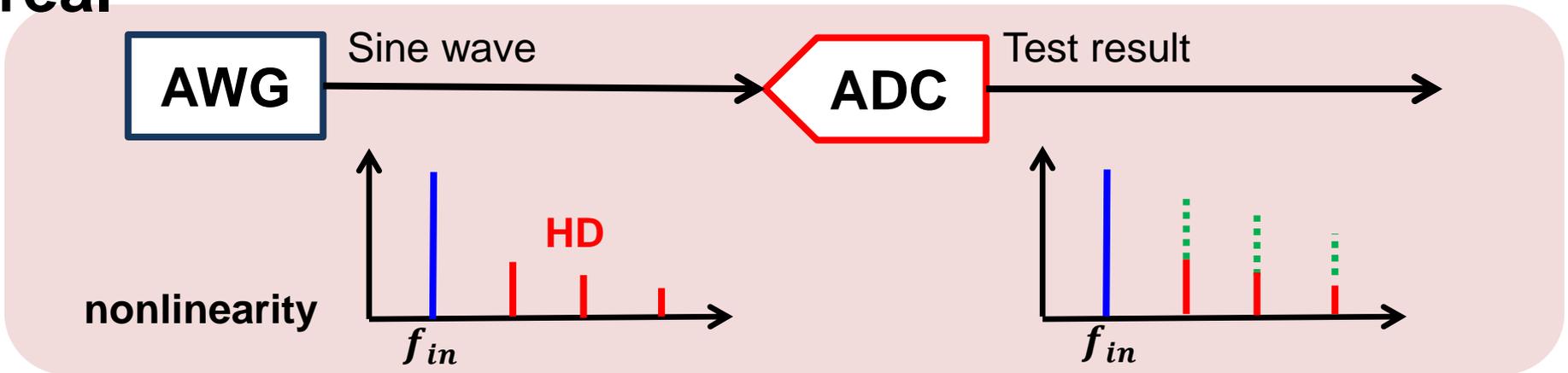
	Cost	Quality
Expensive AWG	✘	○
Low-priced AWG	○	✘
Low-priced AWG + Proposed method	○	○

Ideal and Real

ideal

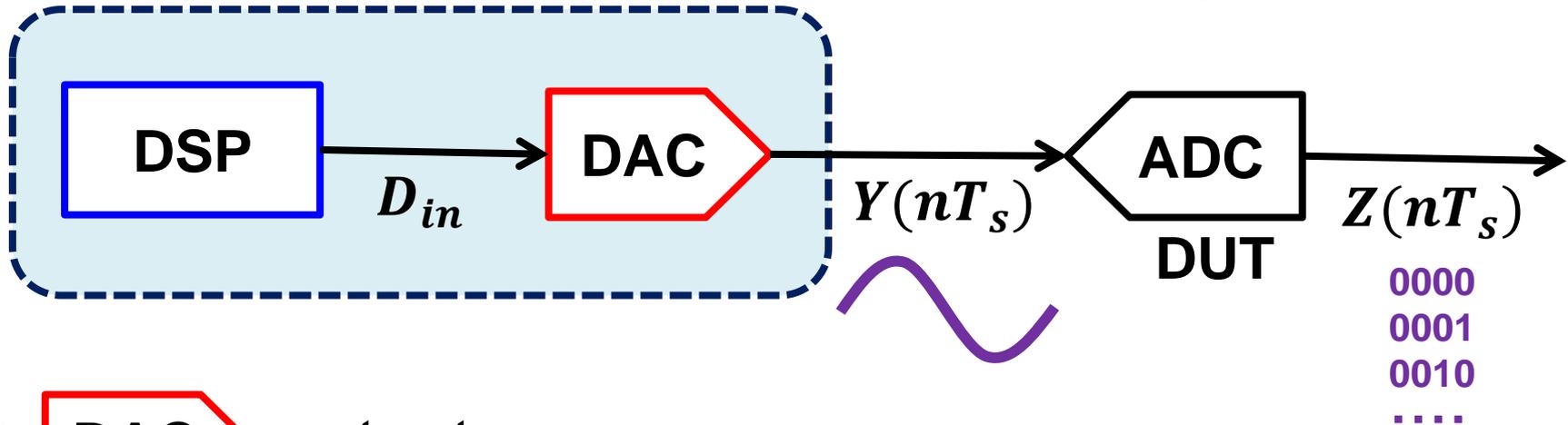


real



Arbitrary Waveform Generator

AWG (Arbitrary Waveform Generator)



- **DAC** output

$$Y(nT_s) = a_1 D_{in} + a_2 D_{in}^2 + a_3 D_{in}^3 + \dots$$

DAC nonlinearity



harmonic distortion



Low-distortion signal generation
Only DSP program change

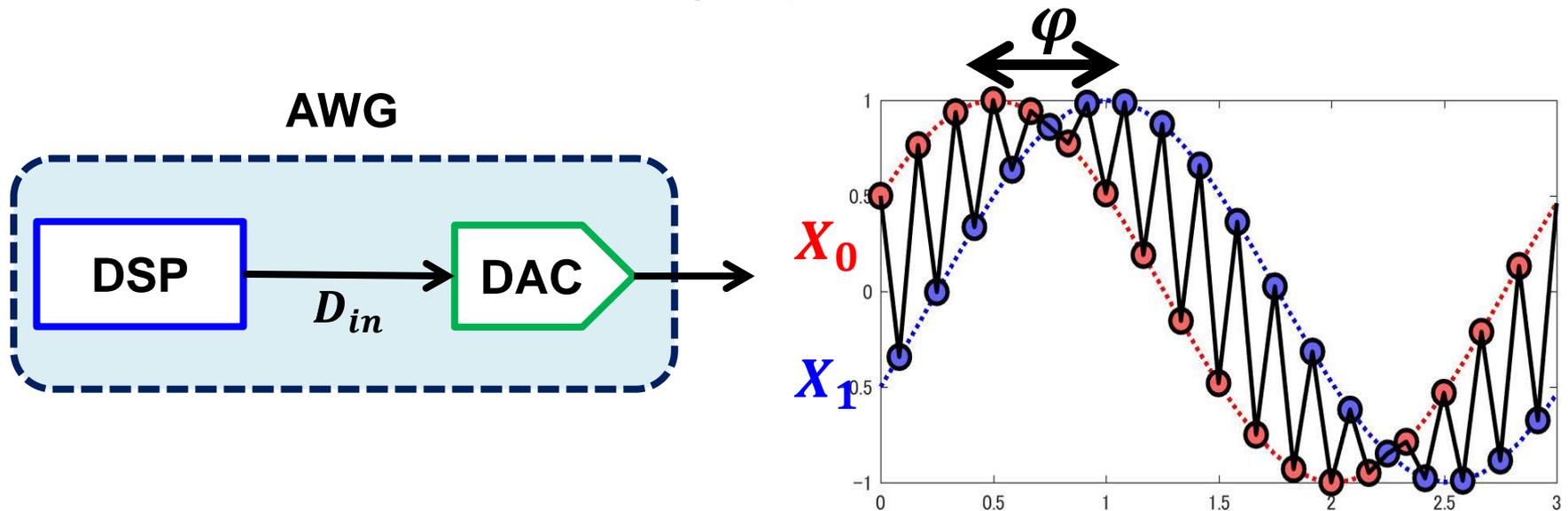
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Our Preceding Study

Phase Switching Signal Method

Interleave sampling X_0 , X_1 every one clock

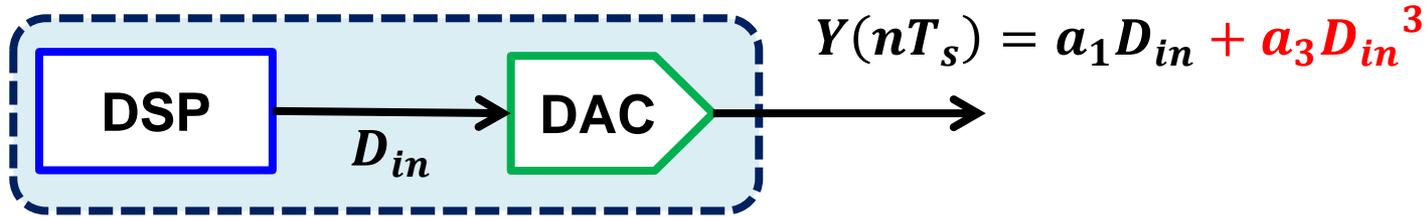


$$D_{in} = \begin{cases} X_0 = A \sin(2\pi f_{in} n T_s + \pi/6) & n: \text{even} \\ X_1 = A \sin(2\pi f_{in} n T_s - \pi/6) & n: \text{odd} \end{cases}$$

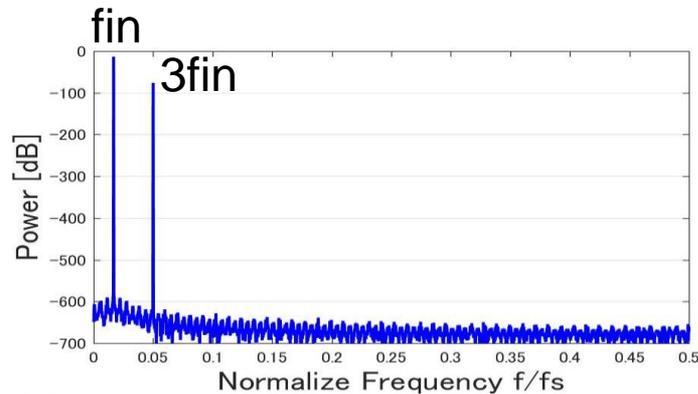
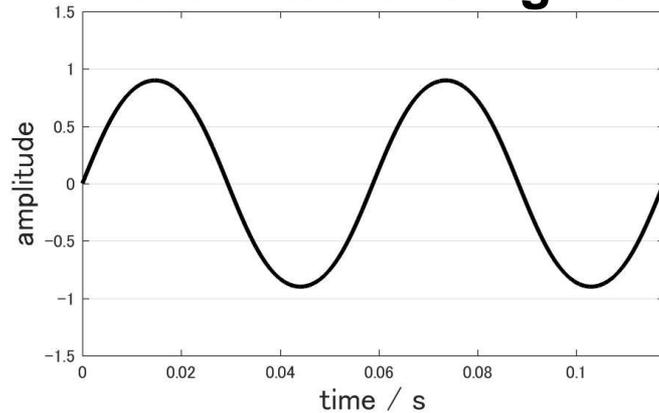
$$\varphi = \varphi_0 - \varphi_1 = \frac{\pi}{3}$$

3rd order harmonics is cancelled

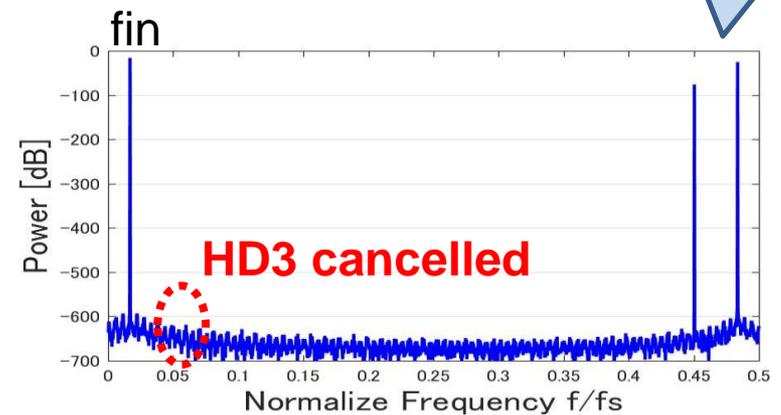
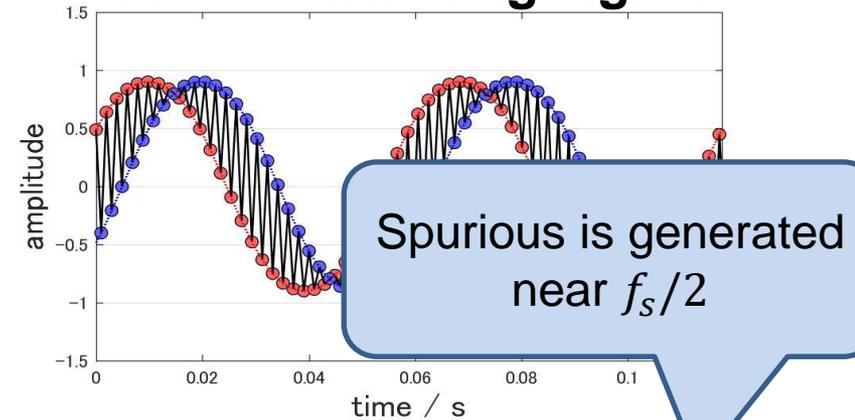
Low-frequency Signal Generation with Phase Switching



Conventional signal



Phase-switching signal



OUTLINE

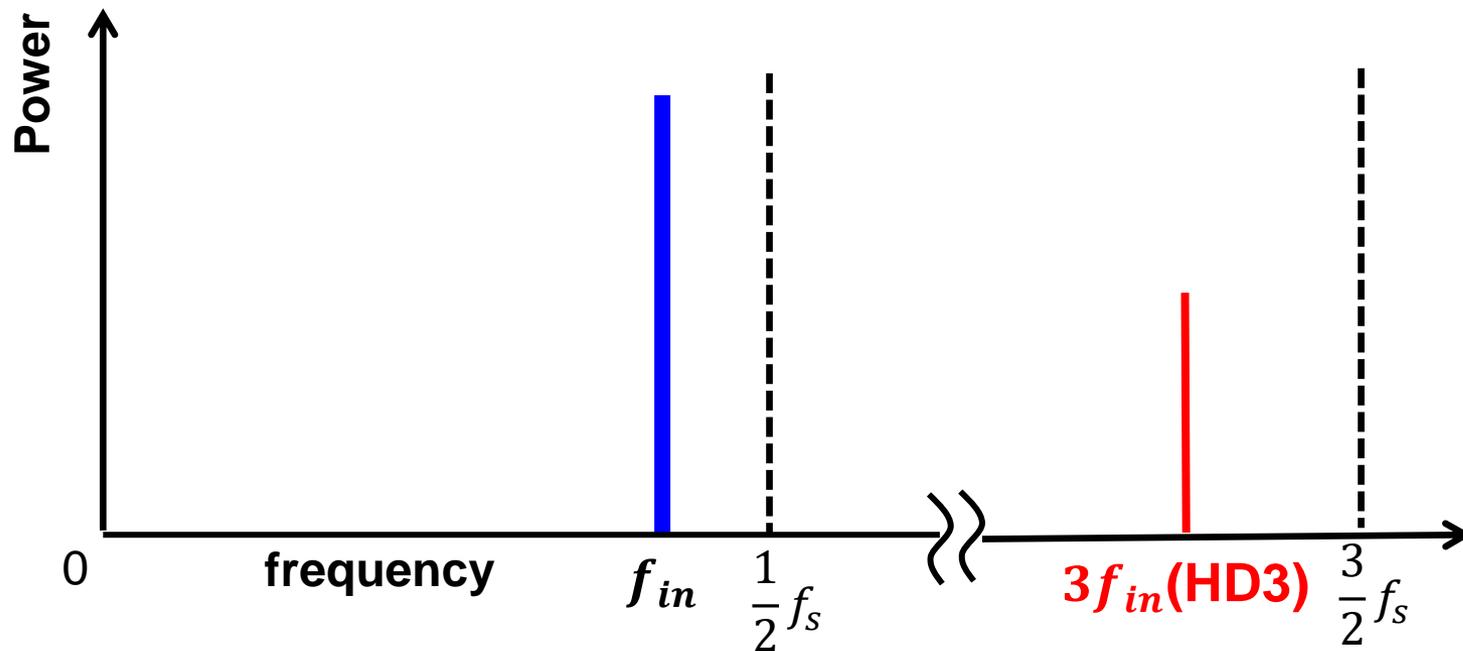
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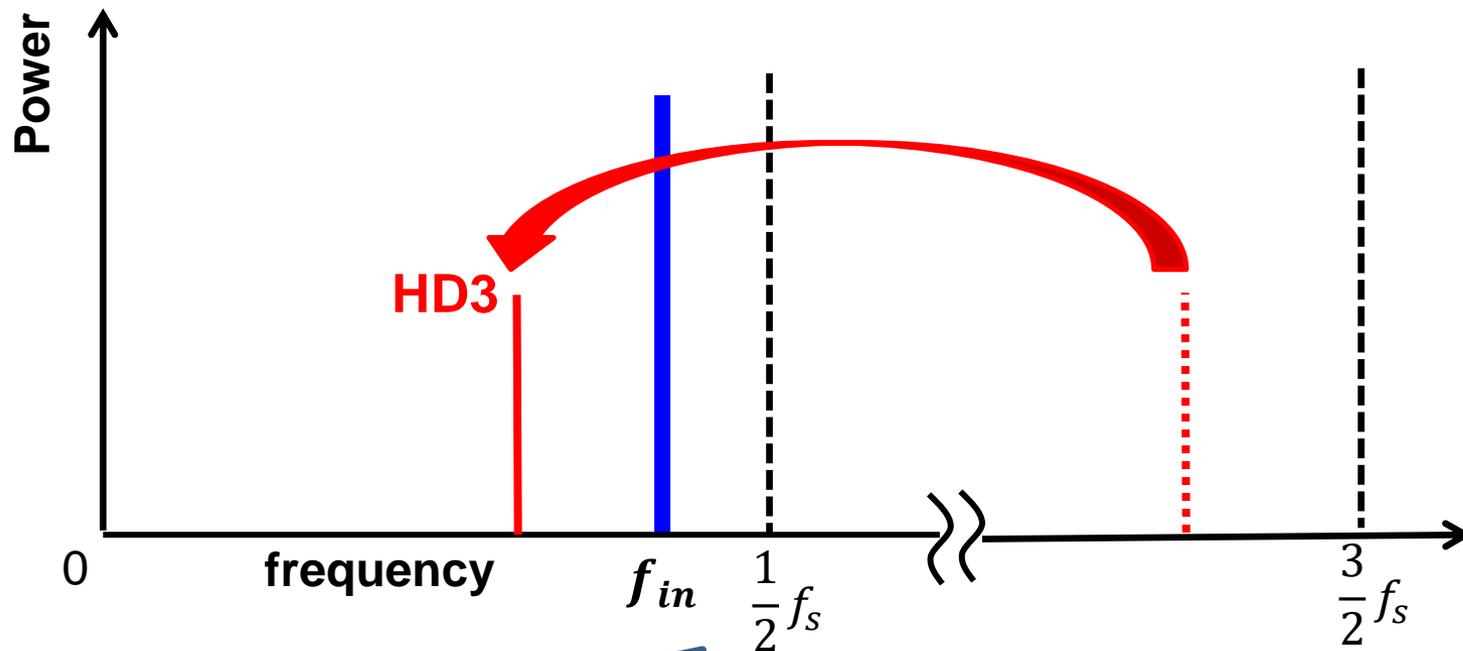
High-frequency Input Case

High-frequency signal = near the Nyquist frequency



High-frequency Input Case

High-frequency signal = near the Nyquist frequency



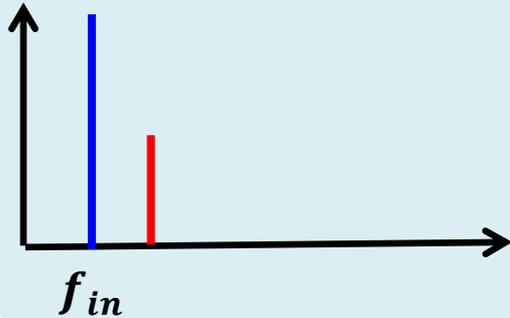
Nyquist frequency

The algorithm is NOT applicable

Algorithm for High-Frequency Signal

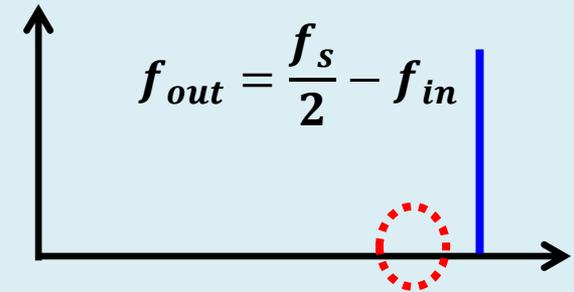
[Input]

Low-frequency
distortional

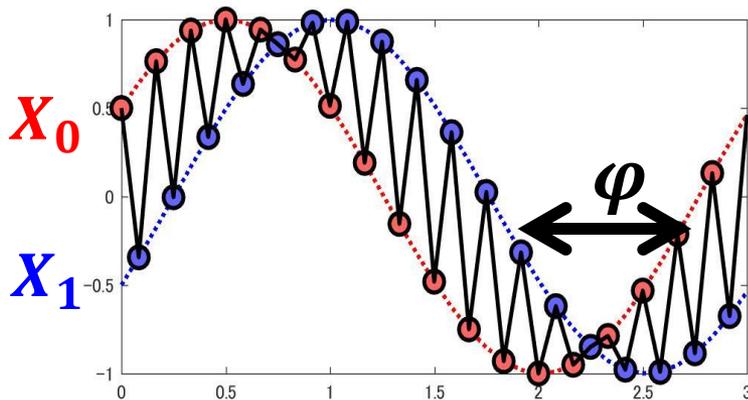


[Output]

High-frequency
Low-distortion



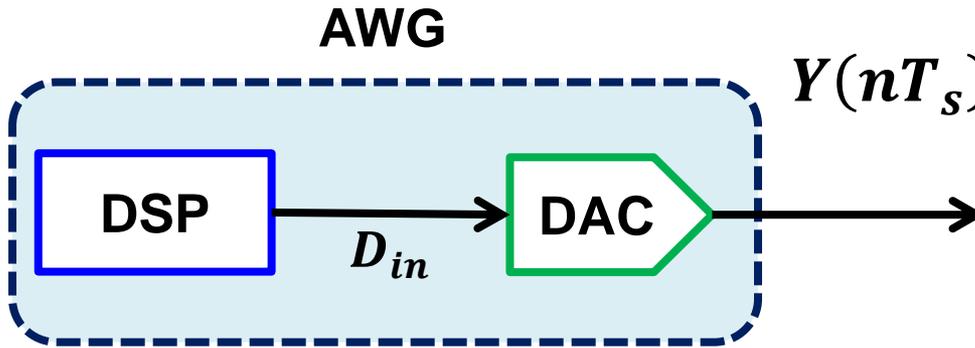
$$D_{in} = \begin{cases} X_0 = A \sin(2\pi f_{in} n T_s + \varphi_0) & n: \text{even} \\ X_1 = A \sin(2\pi f_{in} n T_s - \varphi_1) & n: \text{odd} \end{cases}$$



N th order image is
cancelled

$$\varphi = \varphi_0 - \varphi_1 = \frac{2\pi}{N}$$

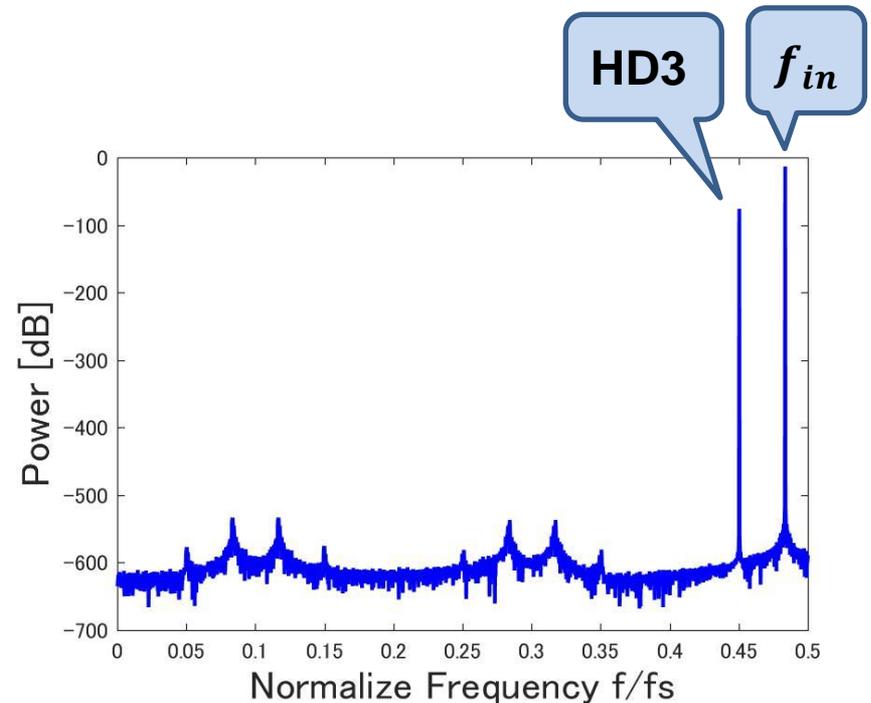
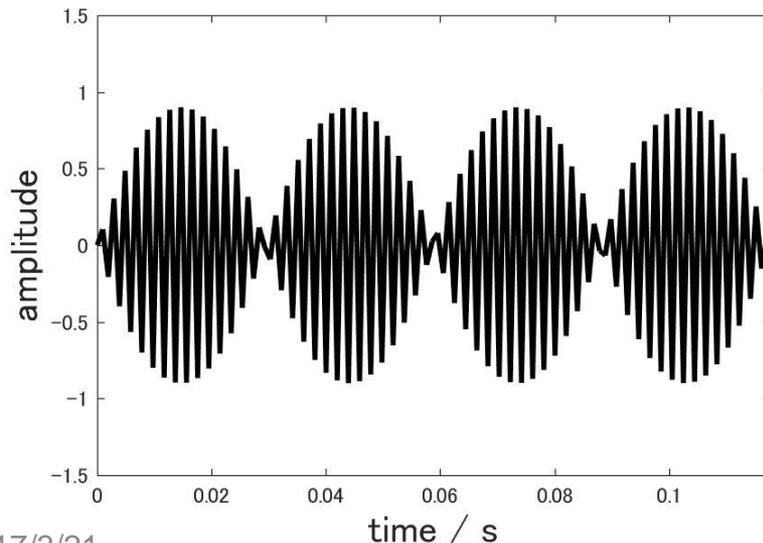
Conventional High-Frequency Signal



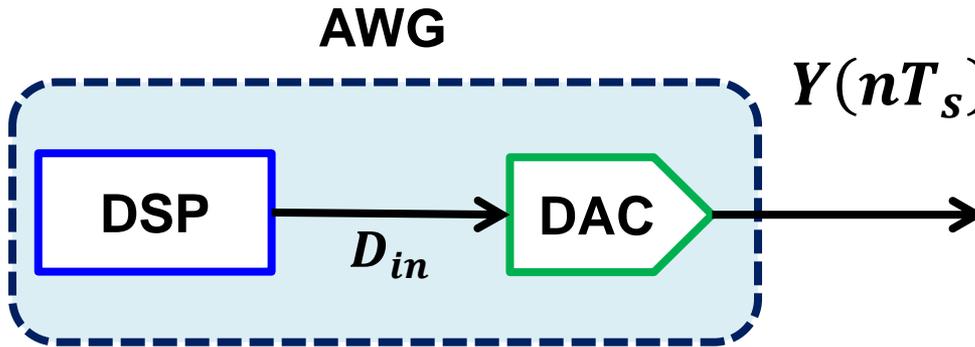
$$Y(nT_s) = a_1 D_{in} + a_3 D_{in}^3$$

f_{in}/f_s	495/1024
a_1, a_3	1, -0.1

$$D_{in} = A \sin(2\pi f_{in} nT_s)$$



Proposed Signal

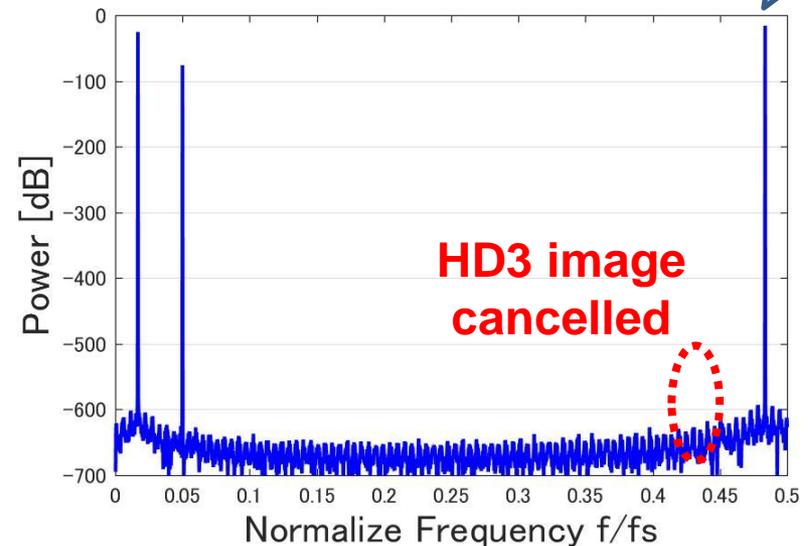
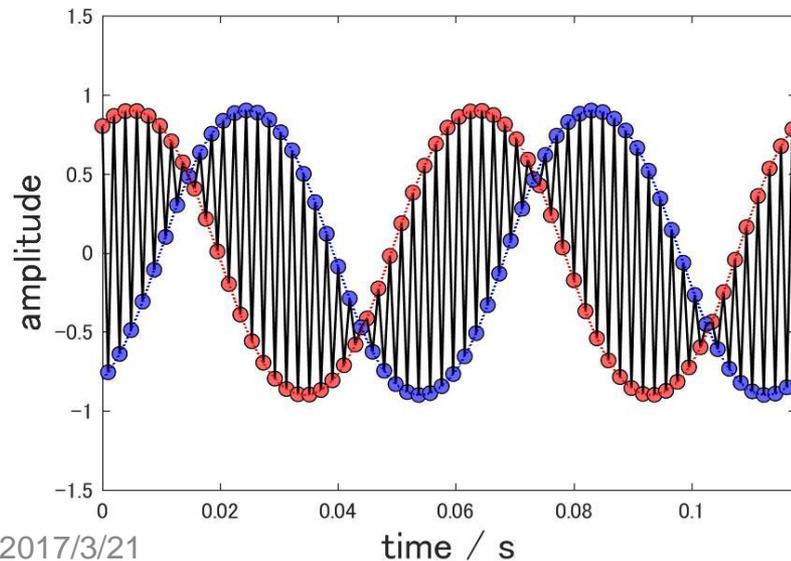


$$Y(nT_s) = a_1 D_{in} + a_3 D_{in}^3$$

f_{in}/f_s	17/1024
a_1, a_3	1, -0.1

$$D_{in} = \begin{cases} X_0 = A \sin(2\pi f_{in} nT_s + \pi/3) & n: \text{even} \\ X_1 = A \sin(2\pi f_{in} nT_s - \pi/3) & n: \text{odd} \end{cases}$$

Signal
 f_{out}



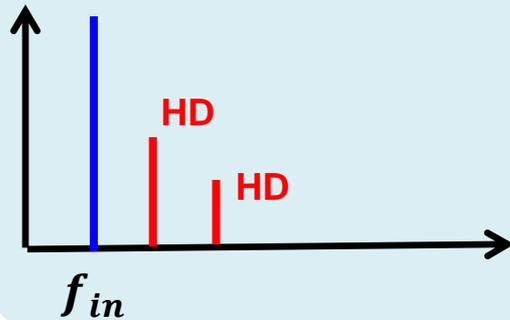
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3rd and 5th Harmonics Cancellation At Once

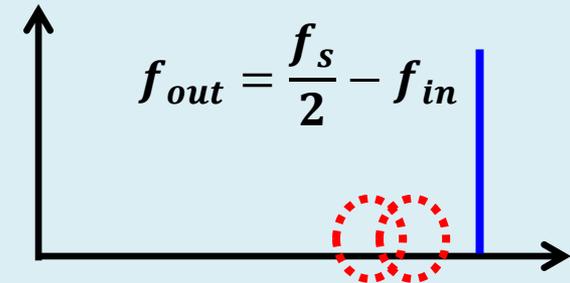
[Input]

Low-frequency
distortional



[Output]

High-frequency
Low-distortion



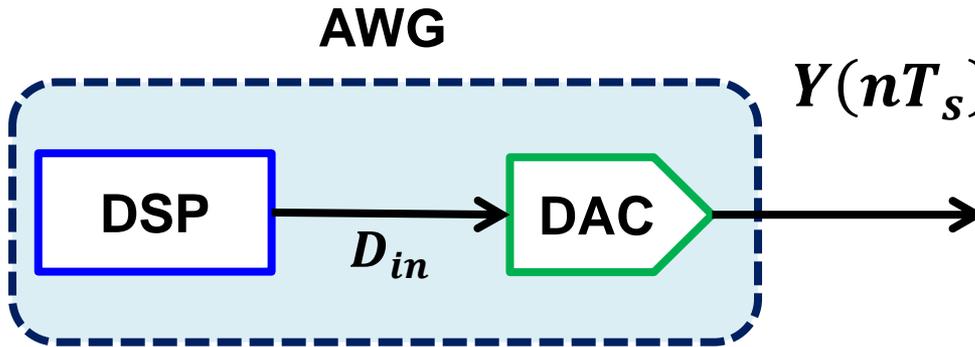
4 phase interleave

$$D_{in} = \begin{cases} X_0 = A \sin(2\pi f_{in} n T_s - \varphi_a - \varphi_b) & n = 4k \\ X_1 = A \sin(2\pi f_{in} n T_s - \varphi_a + \varphi_b) & n = 4k + 1 \\ X_2 = A \sin(2\pi f_{in} n T_s + \varphi_a - \varphi_b) & n = 4k + 2 \\ X_3 = A \sin(2\pi f_{in} n T_s + \varphi_a + \varphi_b) & n = 4k + 3 \end{cases}$$

$$\varphi_a = \frac{\pi}{2N_x} \quad \varphi_b = \frac{\pi}{N_y}$$

Nth order image is cancelled

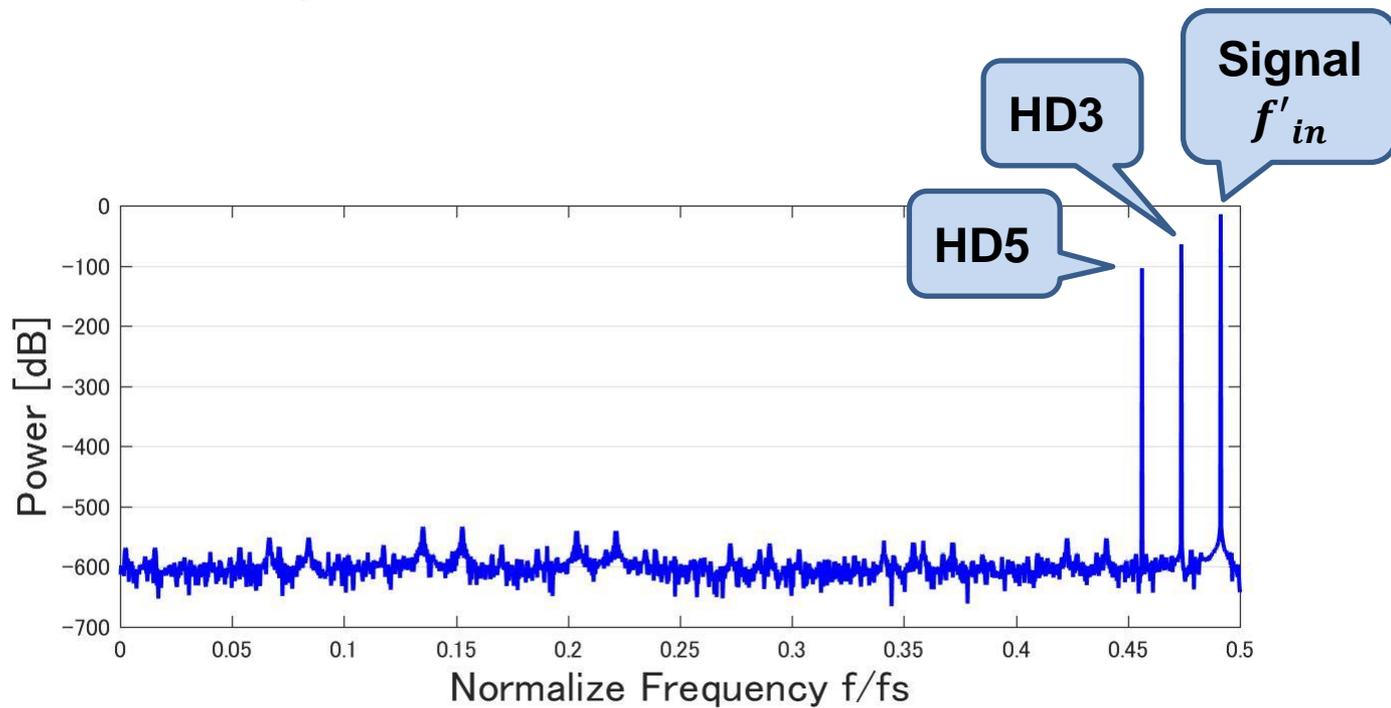
Signal with 3rd and 5th Harmonics



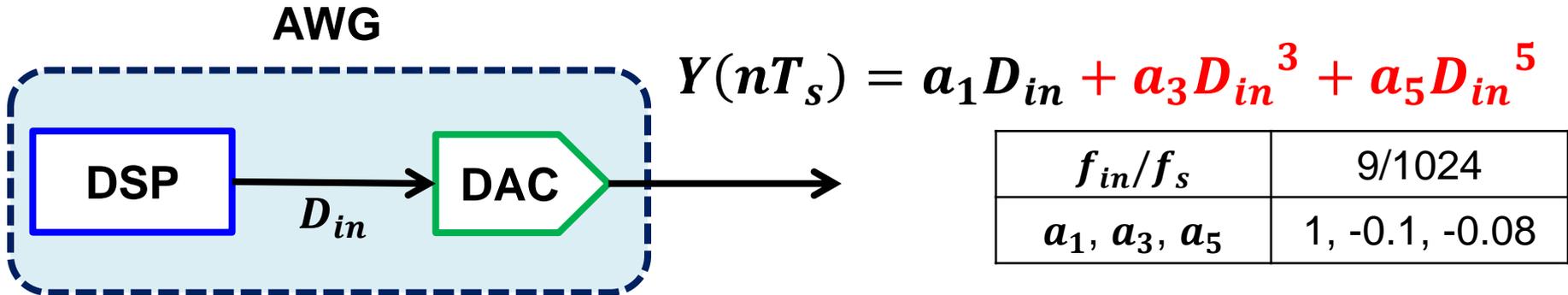
$$Y(nT_s) = a_1 D_{in} + a_3 D_{in}^3 + a_5 D_{in}^5$$

f_{in}/f_s	503/1024
a_1, a_3, a_5	1, -0.1, -0.08

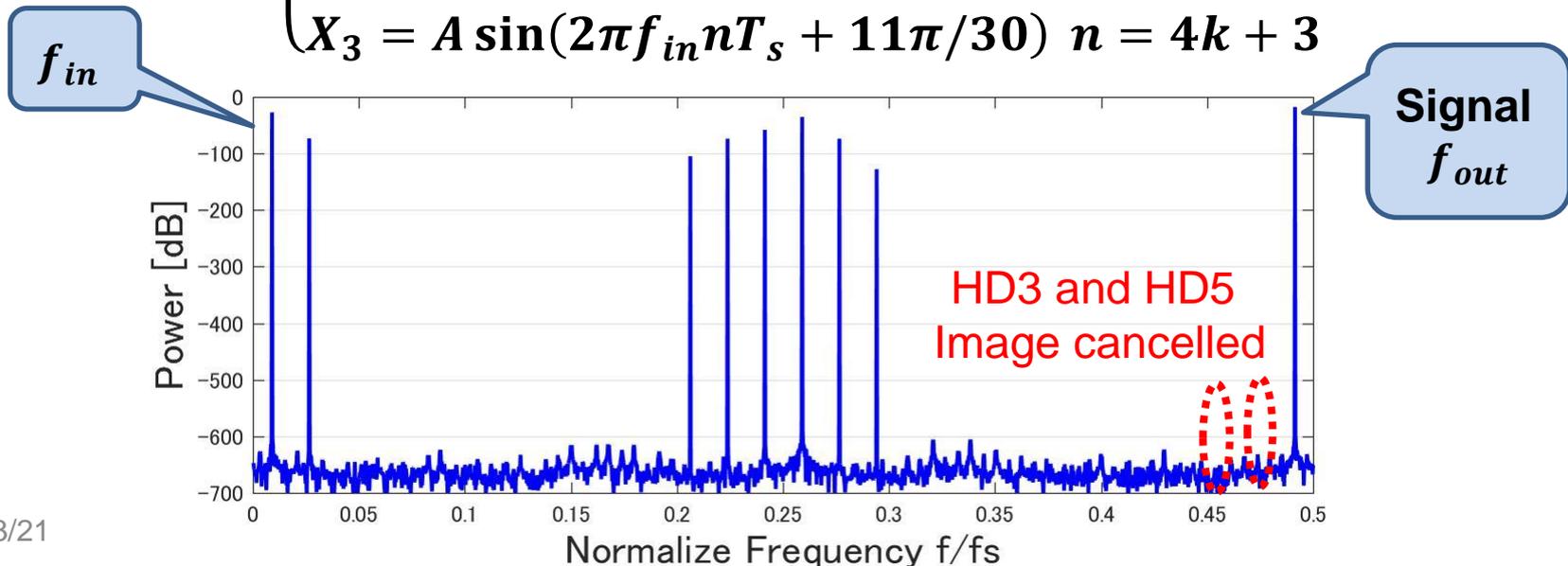
$$D_{in} = A \sin(2\pi f'_{in} nT_s)$$



3rd and 5th Harmonics Cancellation



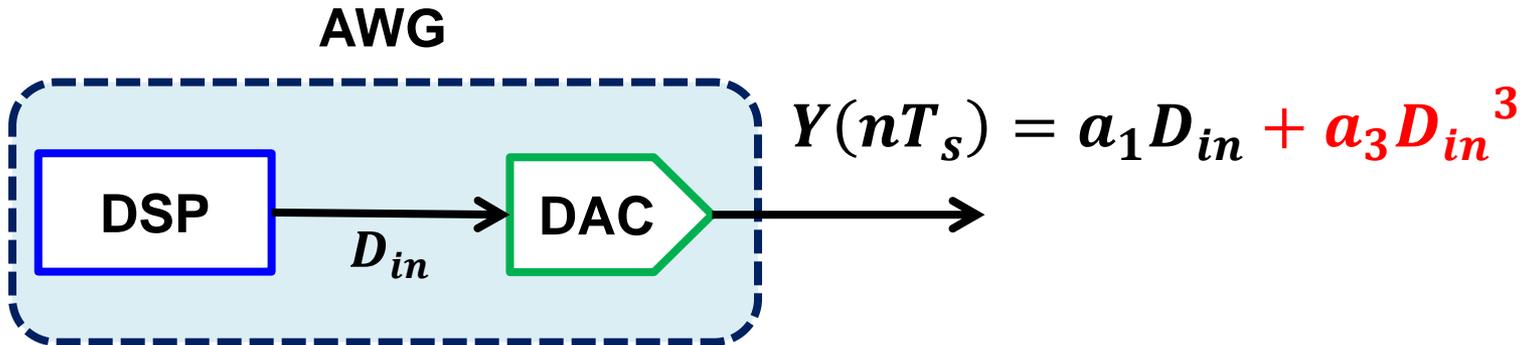
$$D_{in} = \begin{cases} X_0 = A \sin(2\pi f_{in} nT_s - 11\pi/30) & n = 4k \\ X_1 = A \sin(2\pi f_{in} nT_s - \pi/30) & n = 4k + 1 \\ X_2 = A \sin(2\pi f_{in} nT_s + \pi/30) & n = 4k + 2 \\ X_3 = A \sin(2\pi f_{in} nT_s + 11\pi/30) & n = 4k + 3 \end{cases}$$



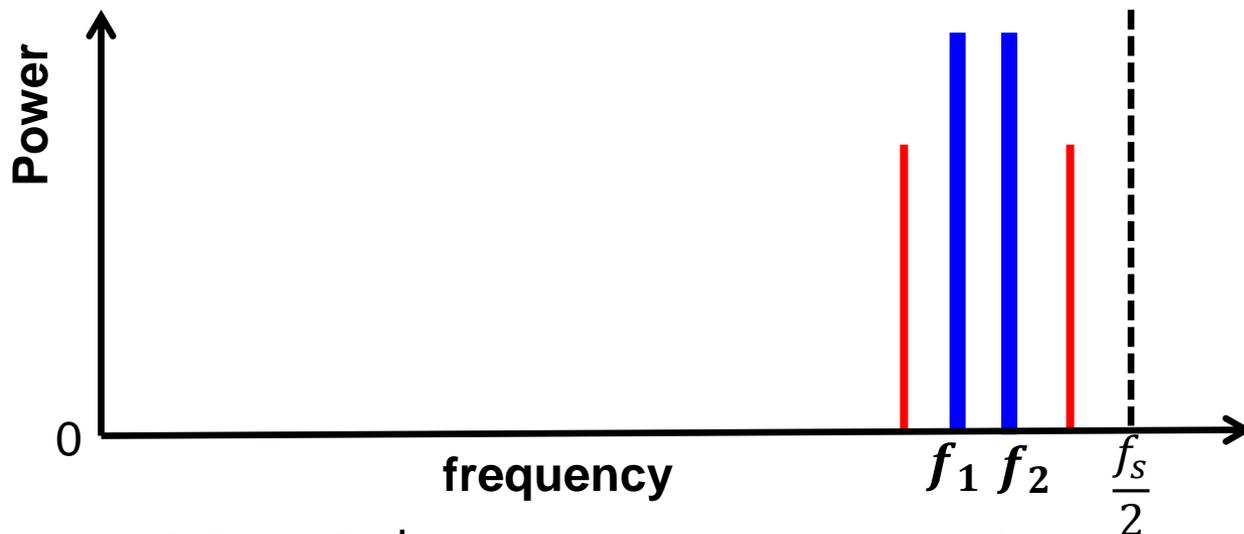
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Two-Tone Signal Case



$$D_{in} = A \sin(2\pi f_1 nT_s) + B \sin(2\pi f_2 nT_s)$$

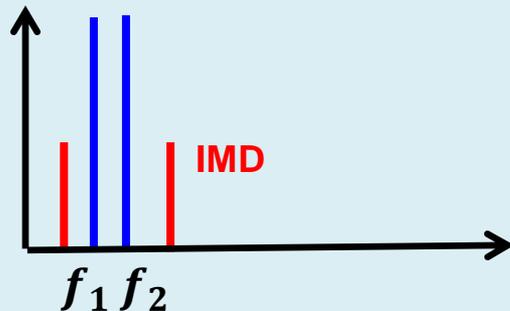


IMD3 = 3rd Intermodulation Distortion

Algorithm For Two-Tone Signals

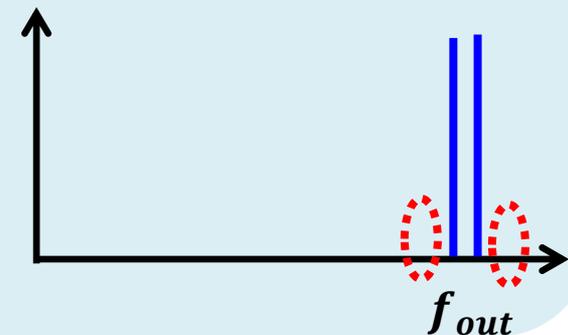
[Input]

Low-frequency
distortional



[Output]

High-frequency
Low-distortion

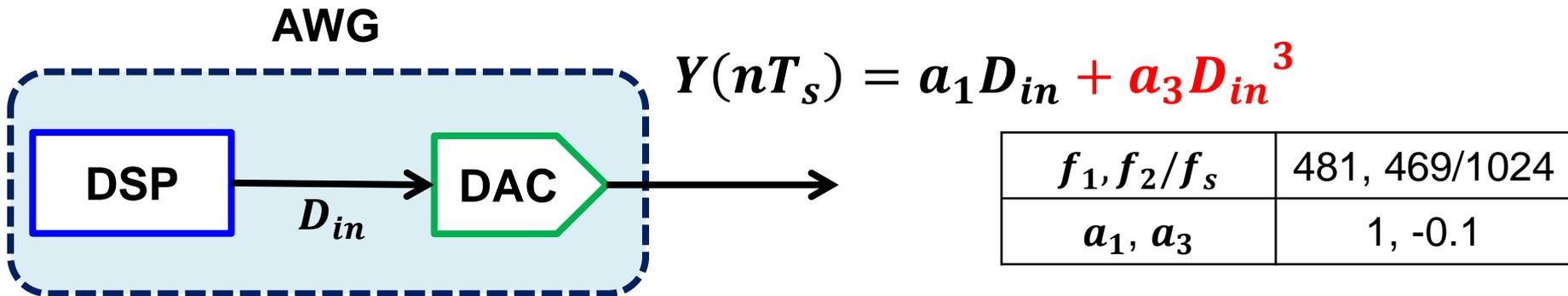


$$D_{in} = \begin{cases} X_0 = A \sin(2\pi f_1 n T_s + \varphi_0) + B \sin(2\pi f_2 n T_s - \varphi_0) & n: \text{even} \\ X_1 = A \sin(2\pi f_1 n T_s - \varphi_0) + B \sin(2\pi f_2 n T_s + \varphi_0) & n: \text{odd} \end{cases}$$

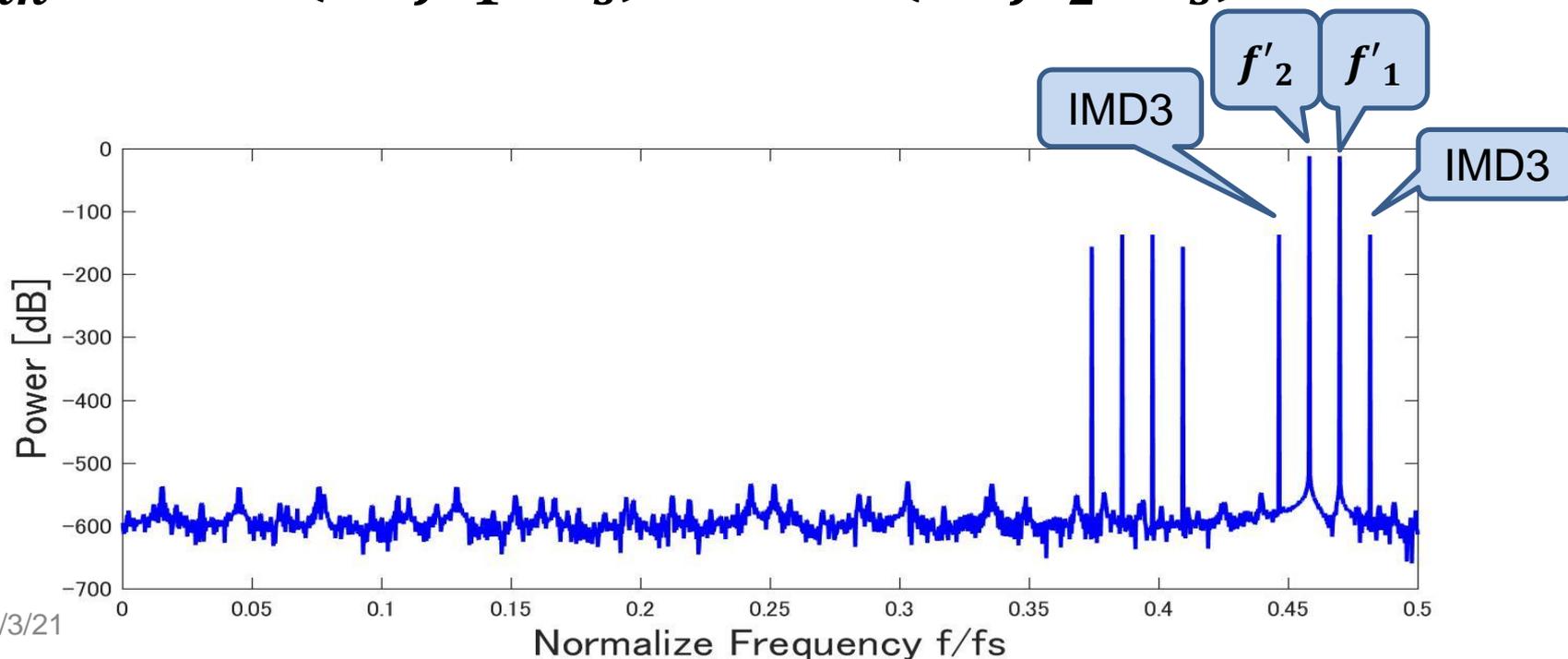
$$\varphi_0 = \frac{\pi}{N}$$

N th order IMD is cancelled

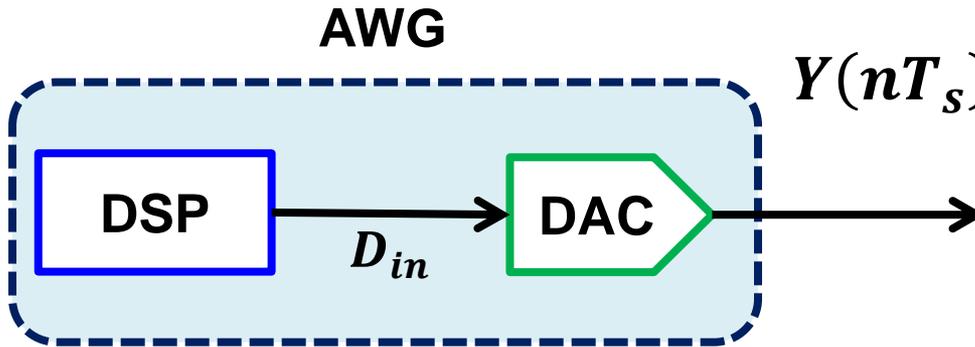
Two-Tone Signal and IMD3



$$D_{in} = A \sin(2\pi f'_1 nT_s) + B \sin(2\pi f'_2 nT_s)$$



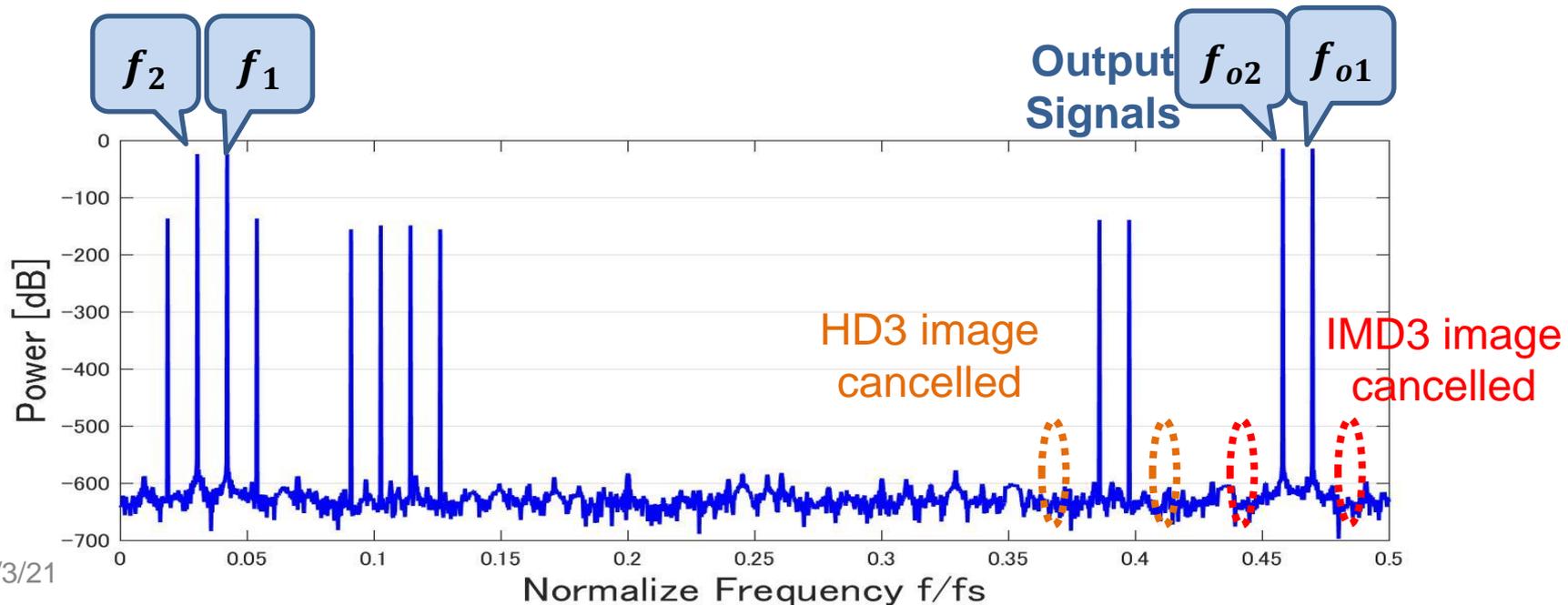
IMD3 Cancellation



$$Y(nT_s) = a_1 D_{in} + a_3 D_{in}^3$$

$f_1, f_2/f_s$	31, 43/1024
a_1, a_3	1, -0.1

$$D_{in} = \begin{cases} X_0 = A \sin(2\pi f_1 nT_s + \pi/3) + B \sin(2\pi f_2 nT_s - \pi/3) & n: \text{even} \\ X_1 = A \sin(2\pi f_1 nT_s - \pi/3) + B \sin(2\pi f_2 nT_s + \pi/3) & n: \text{odd} \end{cases}$$



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Conclusion

- We have proposed high-frequency low-distortion signal generation algorithms with AWG.
- Single-tone and two-tone signal generation
- Need only for a simple analog HPF.
- No need for AWG nonlinearity identification.

**Accurate measurement has
been very important from
thousands years ago**



度量衡 統一 by 始皇帝